

$$1 * \sin x - \sin 15x * \cos x = 3/2$$

$$\sqrt{1 + \sin^2 15x} * (\sin x / \sqrt{1 + \sin^2 15x}) - \sin 15x * \cos x / \sqrt{1 + \sin^2 15x} = 3/2$$

$$1 / \sqrt{1 + \sin^2 15x} = \cos t$$

$$-\sin 15x / \sqrt{1 + \sin^2 15x} = \sin t$$

$$t = t$$

$$\sqrt{1 + \sin^2 15x} * (\sin x * \cos t + \sin t * \cos x) = 3/2$$

$$\sqrt{1 + \sin^2 15x} * \sin(x + t) = 3/2$$

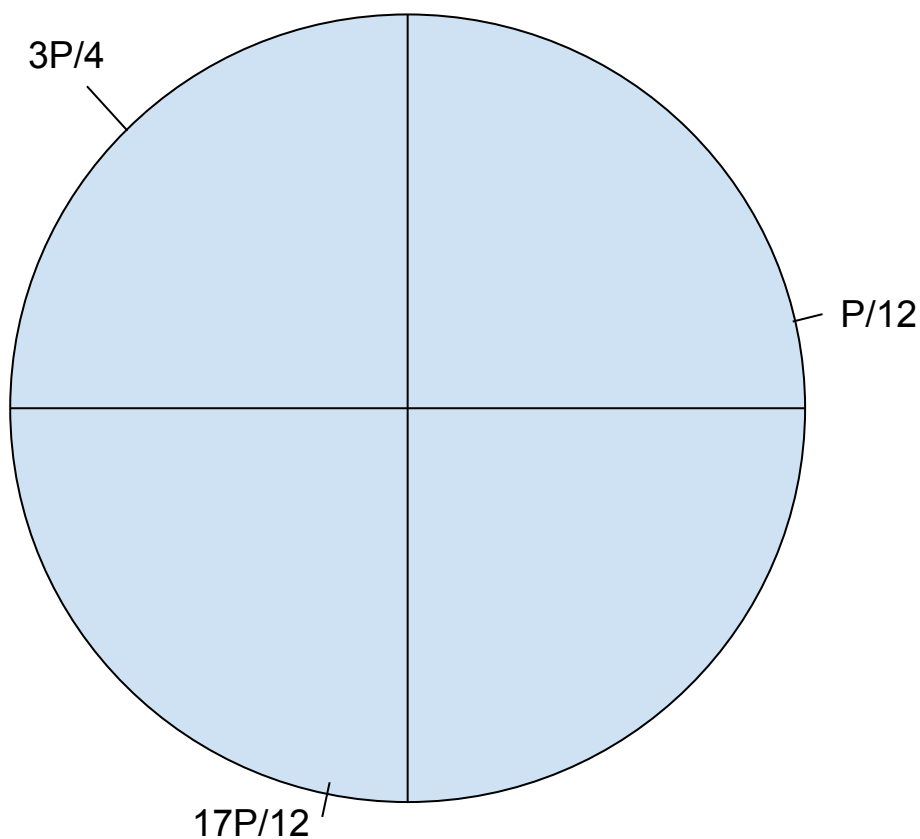
$$-1 \leq \sin(x + t) \leq 1$$

$$0 \leq \sin^2 15x \leq 1$$

$$1 \leq \sqrt{1 + \sin^2 15x} \leq \sqrt{2}$$

$$-\sqrt{2} \leq \sqrt{1 + \sin^2 15x} * \sin(x + t) \leq \sqrt{2}$$

Решений нет



$$\sin 3x - 2\sin 18x * \sin x = 3\sqrt{2} - \cos 3x + 2\cos x$$

$$\sin 3x + \cos 3x = 3\sqrt{2} + 2\sin x * \sin 18x + 2\cos x$$

$$\sqrt{2} * (\sin 3x / \sqrt{2} + \cos 3x / \sqrt{2}) = 3\sqrt{2} + \sqrt{4\sin^2 18x + 4} * (\sin x / \sqrt{4\sin^2 18x + 4} + \cos x / \sqrt{4\sin^2 18x + 4})$$

$$1/\sqrt{2} = \sin t$$

$$1/\sqrt{2} = \cos t$$

$$t = P/4$$

$$\sqrt{4\sin^2 18x + 4} = \sin k$$

$$\sqrt{4\sin^2 18x + 4} = \cos k$$

$$k = k$$

$$\sqrt{2} * (\sin 3x * \cos P/4 + \sin P/4 * \cos 3x) = 3\sqrt{2} + \sqrt{4\sin^2 18x + 4} * (\sin x * \cos k + \sin k * \cos x)$$

$$\sqrt{2} * \sin(3x + P/4) = 3\sqrt{2} + \sqrt{4\sin^2 18x + 4} * \sin(x + k)$$

$$-\sqrt{2} \leq \sqrt{2} * \sin(3x + P/4) \leq \sqrt{2}$$

$$-2 \leq \sqrt{4\sin^2 18x + 4} \leq \sqrt{8}$$

$$-\sqrt{8} \leq \sqrt{4\sin^2 18x + 4} * \sin(x + k) \leq \sqrt{8}$$

$$-2\sqrt{2} + 3\sqrt{2} \leq \sqrt{4\sin^2 18x + 4} * \sin(x + k) + 3\sqrt{2} \leq 2\sqrt{2} + 3\sqrt{2}$$

$$\sqrt{2} \leq \sqrt{4\sin^2 18x + 4} * \sin(x + k) + 3\sqrt{2} \leq 5\sqrt{2}$$

Левая и правая части могут быть равны, только когда каждая из них - это $\sqrt{2}$

$$\sqrt{2} * \sin(3x + P/4) = \sqrt{2}$$

$$\sin(3x + P/4) = 1$$

$$3x + P/4 = P/2 + 2Pn$$

$$3x = P/4 + 2Pn$$

$$x = P/12 + 2Pn/3$$

$$P/12 + 2P/3 = P/12 + 8P/12 = 9P/12 = 3/4 * P$$

$$P/12 + 4P/3 = P/12 + 16P/12 = 17P/12$$

$$x_1 = P/12 + 2Pn$$

$$x_2 = 3P/4 + 2Pn$$

$$x_3 = 17P/12 + 2Pn$$

Проверим эти серии на равенство $\sqrt{2}$ правой части методом подстановки (подставлять будем в начальный вид правой части $3\sqrt{2} + 2\sin x * \sin 18x + 2\cos x$):

$$\begin{aligned} x_1: & 3\sqrt{2} + 2 * \sin(P/12 + 2Pn) * \sin(18P/12 + 36Pn) + 2\cos(P/12 + 2Pn) = 3\sqrt{2} + 2 * \sin P/12 * \sin 3P/2 + 2 * \cos P/12 = \\ & 3\sqrt{2} - 2\sin P/12 + 2\cos P/12 = 3\sqrt{2} - 2(\sin P/12 - \cos P/12) = 3\sqrt{2} - 2\sqrt{2}(\sin P/12(\sqrt{2}/2) - \cos P/12(\sqrt{2}/2)) = \\ & = 3\sqrt{2} - 2\sqrt{2}(\sin P/12 * \cos P/4 - \cos P/12 * \sin P/4) = 3\sqrt{2} - 2\sqrt{2} * \sin(P/12 - P/4) = 3\sqrt{2} - 2\sqrt{2} * \sin(-P/6) = \\ & = 3\sqrt{2} - 2\sqrt{2} * (-1/2) = 4\sqrt{2} \neq \sqrt{2} \Rightarrow \mathbf{x_1 \text{ не подходит}} \end{aligned}$$

$$x_2:$$

$$3\sqrt{2} + 2\sin(3P/4 + 2Pn) * \sin(54P/4 + 36Pn) + 2\cos(3P/4 + 2Pn) = 3\sqrt{2} + 2 * \sin 3P/4 * \sin 54P/4 + 2 * \cos 3P/4 =$$

$$= 3\sqrt{2} + \sqrt{2} * \sin 54P/4 - \sqrt{2} = \sqrt{2}(2 + \sin 54P/4) = \sqrt{2}(2 + \sin 27P/2) = \sqrt{2}(2 + \sin(27P/2 - 24P/2)) = \sqrt{2}(2 + \sin(3P/2)) = \sqrt{2}(2 - 1) = \sqrt{2} - \mathbf{ПОДХОДИТ}$$

$$x_3:$$

$$3\sqrt{2} + 2 * \sin(17P/12 + 2Pn) * \sin(51P/2 + 36Pn) + 2 * \cos(17P/12 + 2Pn) = 3\sqrt{2} + 2 * \sin 17P/12 * \sin 51P/2 + 2 * \cos 17P/12 = 3\sqrt{2} + 2 * \sin 17P/12 * \sin(51P/2 - 48P/2) + 2 * \cos 17P/12 = 3\sqrt{2} + 2 * \sin 17P/12 * \sin(3P/2) + 2 * \cos 17P/12 = 3\sqrt{2} - 2 * \sin 17P/12 + 2 * \cos 17P/12 = 3\sqrt{2} - 2 * (\sin 17P/12 - \cos 17P/12) = 3\sqrt{2} - 2 * \sqrt{2} * (\sin 17P/12 * 1/\sqrt{2} - \cos 17P/12 * 1/\sqrt{2}) = 3\sqrt{2} - 2\sqrt{2} * (\sin 17P/12 * \cos P/4 - \sin P/4 * \cos 17P/12) = 3\sqrt{2} - 2\sqrt{2} * \sin(17P/12 - P/4) = 3\sqrt{2} - 2\sqrt{2} * \sin 7P/6 = 3\sqrt{2} + \sqrt{2} = 4\sqrt{2} \Rightarrow \mathbf{x_3 \text{ не подходит}}$$

Ответ: $3P/4 + 2Pn$